

Research Article

# Design of O-Ring with No-Groove Arrangement

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## Abstract

The O-rings are the very commonly employed solution for creating sealing to prevent the loss of pressurized fluid or gases. In the present work the design of an O-ring with no-groove arrangement is presented.

**Keywords:** Lubricated O-ring, Un-lubricated O-ring, Sealing, Design, Leakage, Elastomers

## 1. Introduction

The loss of pressurized fluid or gas is generally prevented by the use of O-rings. The O-rings are made up of elastomeric materials. The sealing effect in these elastomers occurs due to their axial or radial compression. The elastomer behaves as an incompressible liquid of great viscosity with high surface tension [1]. When the O-ring is installed in such a way that no groove has been provided in the assembly, then this type of arrangement is called no groove arrangement [2]. There are two types of no groove arrangement, depending upon the type of compression being imposed upon the O-ring, the Axial O-ring and Radial O-ring [3].

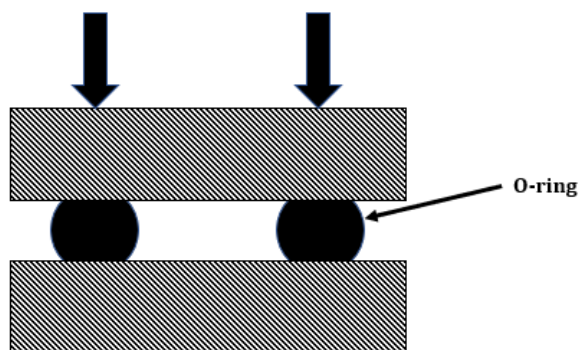


Fig.1 Axially loaded O-ring without groove

The no groove arrangement for the axial loaded O-ring is depicted in figure 1. Under the case of axial compression, the O-ring is free to expand radially as a result of which the corresponding shape of the O-ring under load changes as shown in the figure 2.

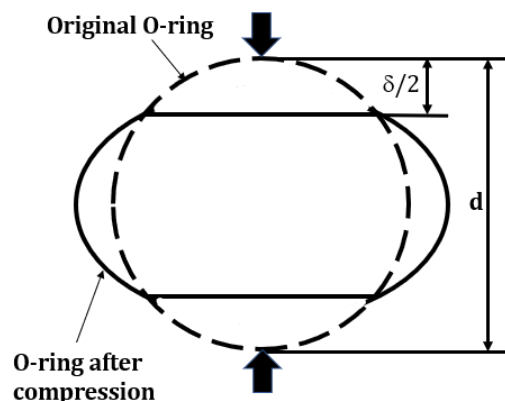


Fig. 2 Deformed O-ring

The compression brings out a change in the cross-sectional diameter of the O-ring, from an initial value of 'd'[2]. In order to define the change in the diameter, a parameter called as compression ratio ( $\psi$ ) is introduced which is defined as the change in the cross-sectional diameter divided by the original cross-sectional diameter.

$$\psi = \frac{\text{Change in cross-sectional diameter}}{\text{Original diameter}} \quad (1)$$

The analysis of the O-ring has been divided into two categories, namely: (i) Unlubricated condition and (ii) Lubricated condition based upon whether lubrication was provided to the O-ring prior to its installation within the assembly or not [4], [5], [14]–[23], [6], [24]–[33], [7], [34]–[43], [8], [44]–[53], [9], [54]–[63], [10], [64]–[69], [11]–[13]. Lubrication may result in swelling up of the O-ring, which increases the cross-section diameter of the O-ring.

## 2. Axially Loaded Unlubricated Condition

The unlubricated condition specifies the situation when the O-ring has been installed in the assembly without

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prior lubrication around the surface of the O-ring. In static applications, where movement between the sealing faces and the O-ring is negligible, unlubricated O-rings can be utilized without significantly affecting the life of the O-ring.

Squeeze upon loading: The O-ring under compression will undergo an effective squeeze defined as the change in its cross-section which is calculated from the compression ratio ( $\psi$ ) and O-ring diameter ( $d$ ).

The formulation is given in equation 2.

$$squeeze = \psi * d \tag{2}$$

There are two approaches for the calculation of Young's Modulus.: Young's Modulus determination using hardness and the other using stress and strain values

Young's Modulus determination using hardness: The estimation for Young's Modulus has been formulated using the value of hardness as a parameter using the empirical relation proposed:

$$E = 0.256 * e^{0.047*(hardness-hardtol)} \tag{3}$$

$$E = 0.256 * e^{0.047*(hardness+hardtol)} \tag{4}$$

When calculating Young's Modulus using hardness, both positive and negative tolerances have been utilized in the O-ring design leading to two different values of Young's Modulus. Under the same compression imposed upon the O-ring, positive tolerances on hardness yield a higher value of Young's Modulus and consequently the stresses generated on the O-ring will be higher and vice versa. Therefore, for calculating the stress, positive tolerance of O-Ring is considered and in the case of safeguard against leakage/squeezing out, calculation of Young's Modulus using negative tolerances is incorporated.

Young's Modulus determination using stress and strain values: The estimation of Young's Modulus using hardness as a parameter is based on an empirical relation and therefore, in order to estimate a more accurate value of Young's Modulus, stress and strain values, which have been arrived experimentally are preferred.

The relation between stress and strain for hyper-elastic rubber materials such as O-ring is non-linear, and several models have been proposed from time to time in order to evaluate the value of Young's Modulus using stress and strain.

According to Cauchy-Green, the stretch imparted to any material can be expressed by using three invariants as represented below:

$$I_1 = \lambda_1^2 + \lambda_2^2 + \lambda_3^2 \tag{5}$$

$$I_2 = \lambda_1^2 \lambda_2^2 + \lambda_2^2 \lambda_3^2 + \lambda_1^2 \lambda_3^2 \tag{6}$$

$$I_3 = \lambda_1^2 \lambda_2^2 \lambda_3^2 \tag{7}$$

Where  $\lambda$  represents the stretch and is defined as:

$$\lambda = \frac{Deformed\ Length}{Undeformed\ Length}$$

$$\lambda = 1 - \epsilon \tag{8}$$

$\epsilon$  - Representing the strain in the material.

The three invariants specifically represent the change in length, surface area and volume of the hyper-elastic material.

Since the material is assumed to be incompressible, therefore:

$$\lambda_1 \lambda_2 \lambda_3 = 1 \tag{9}$$

Mooney-Rivlin model: The Mooney-Rivlin model uses a linear combination of two invariants of the Cauchy-Green deformation tensor in the definition of the strain energy density function ( $W$ ) which is defined as follows:

$$W = C_1(I_1 - 3) + C_2(I_2 - 3) \tag{10}$$

For the case of uniaxial tension or compression imparted to the O-ring, the following values can be used:

$$\lambda_1 = \lambda \tag{11}$$

$$\lambda_2 = \frac{1}{\sqrt{\lambda}} \tag{12}$$

$$\lambda_3 = \frac{1}{\sqrt{\lambda}} \tag{13}$$

Using these values

$$I_1 = \lambda^2 + \frac{2}{\lambda} \tag{14}$$

$$I_2 = \lambda + \frac{2}{\lambda^2} + \lambda \tag{15}$$

On substituting these values in Eq. (10),

$$W = C_1 \left( \lambda^2 + \frac{2}{\lambda} - 3 \right) + C_2 \left( \lambda + \frac{1}{\lambda^2} + \lambda - 3 \right) \tag{16}$$

The differentiation of the above equation with respect to  $\lambda$  yields the value of stress. Therefore, on differentiating with respect to  $\lambda$ , we have:

$$\frac{dW}{d\lambda} = C_1 \left( 2\lambda - \frac{2}{\lambda^2} \right) + C_2 \left( 2 - \frac{2}{\lambda^3} \right) \tag{17}$$

$$f = \frac{dW}{d\lambda} = 2 C_1 \left( \lambda - \frac{1}{\lambda^2} \right) + 2 C_2 \left( 1 - \frac{1}{\lambda^3} \right) \tag{18}$$

$$f = 2 \left( C_2 + C_1 \lambda \right) \left( 1 - \frac{1}{\lambda^3} \right) \tag{19}$$

Equation (2.11) can be rewritten as

$$f = 2 \left( C_1 + \frac{C_2}{\lambda} \right) \left( \lambda - \frac{1}{\lambda^2} \right) \tag{20}$$

Where  $f$  denotes the Cauchy stress and  $C_2$  and  $C_1$  are material constants. The values of material constant are estimated by curve fitting the stress ( $f$ ) and stretch ( $\lambda$ ) values from the obtained experimental results. In the present work least-square method is adopted for curve fitting the stress and stretch values. The detail discussion of the method opted is discussed in detail below. The least squared approach is based upon the minimization of the square of the error between the function and estimated values.

For example, in the present case

$$2 \left( C_1 + \frac{C_2}{\lambda} \right) \left( \lambda - \frac{1}{\lambda^2} \right)$$

is the function and stress “*f*” is the estimated value. Therefore, the equation (20) can be rewritten as:

$$\text{minimize } err = \sum_{i=1}^n \left( f_i - 2 \left( C_1 + \frac{C_2}{\lambda} \right) \left( \lambda - \frac{1}{\lambda^2} \right) \right)^2 \quad (21)$$

$$\text{minimize } err = \sum_{i=1}^n \left( f_i - 2 \left( C_1 \lambda + C_2 - \frac{C_1}{\lambda^2} - \frac{C_2}{\lambda^3} \right) \right)^2 \quad (22)$$

Where

*err* –the error involved while curve fitting

*i* – Current data point being summed

*n* – No. of data points given

*f<sub>i</sub>* – Stress at data point *i* [MPa]

Now calculate the derivatives of the function “*err*” (i.e. equation (22)) with respect to the two constants *C*<sub>1</sub> and *C*<sub>2</sub>, and set both these equations equal to zero.

$$\frac{\partial err}{\partial C_1} = \left( \sum_{i=1}^n -2 \left( f_i - 2 \left( C_1 \lambda_i + C_2 - \frac{C_1}{\lambda_i^2} - \frac{C_2}{\lambda_i^3} \right) \right) 2 \left( \lambda_i - \frac{1}{\lambda_i^2} \right) \right) = 0 \quad (23)$$

$$\frac{\partial err}{\partial C_2} = \left( \sum_{i=1}^n -2 \left( f_i - 2 \left( C_1 \lambda_i + C_2 - \frac{C_1}{\lambda_i^2} - \frac{C_2}{\lambda_i^3} \right) \right) 2 \left( 1 - \frac{1}{\lambda_i^3} \right) \right) = 0 \quad (24)$$

Rewriting the above two equations, we obtain:

$$\sum_{i=1}^n f_i \left( \lambda_i - \frac{1}{\lambda_i^2} \right) - 2C_1 \sum_{i=1}^n \left( \lambda_i^2 - \frac{2}{\lambda_i} + \frac{1}{\lambda_i^4} \right) - 2C_2 \sum_{i=1}^n \left( \lambda_i - \frac{2}{\lambda_i^2} + \frac{1}{\lambda_i^5} \right) = 0 \quad (25)$$

$$\sum_{i=1}^n f_i \left( 1 - \frac{1}{\lambda_i^3} \right) - 2C_1 \sum_{i=1}^n \left( \lambda_i - \frac{2}{\lambda_i^2} + \frac{1}{\lambda_i^5} \right) - 2C_2 \sum_{i=1}^n \left( n - \frac{2}{\lambda_i^3} + \frac{1}{\lambda_i^6} \right) = 0 \quad (26)$$

Simultaneously solving equations 25 and 26 by substituting the values of ‘*f*’ and ‘*λ*’, the values of *C*<sub>1</sub> and *C*<sub>2</sub> are obtained. The values of stress obtained using the Mooney-Rivlin model has been calculated above.

Apart from the Mooney-Rivlin model, there are two other models available to estimate the Young’s Modulus using the Stress vs Stretch plot (i) Hooke’s model and (ii) Neo-Hookean Model.

Hooke’s model: Hooke’s law states that the stress is proportion to the stretch and the relation between the two has been shown in equation (27).

$$f = C_{10} \lambda \quad (27)$$

Where,

*f*= Stress value and

*λ*= Stretch value.

The values of stress obtained using the Hooke’s model has been calculated.

Neo-Hookean model: Neo-Hookean model is a hyper elastic material model that can be used for predicting the stress-strain behavior of materials, and the model is similar to Hooke’s law. The strain energy density function is described as follows:

$$W = C_{10}(I_1 - 3) \quad (28)$$

The O-ring is assumed to be incompressible, therefore, using the Cauchy Stress Invariant *I*<sub>3</sub>, is given by:

$$\lambda_1 \lambda_2 \lambda_3 = 1 \quad (29)$$

For the case of uniaxial tension or compression imparted to the O-ring the following values are used:

$$\lambda_1 = \lambda \quad (30)$$

$$\lambda_2 = \frac{1}{\sqrt{\lambda}} \quad (31)$$

$$\lambda_3 = \frac{1}{\sqrt{\lambda}} \quad (32)$$

Therefore, the Strain Energy Density function can be written as:

$$W = C_{10} \left( \lambda^2 + \frac{2}{\lambda} - 3 \right) \quad (33)$$

For an incompressible Neo-Hookean material, therefore, differentiating the strain energy density function with respect to *λ*.

$$f = 2C_{10} \left( \lambda - \frac{1}{\lambda^2} \right) \quad (34)$$

*C*<sub>10</sub>= Material constant (Neo-Hookean constant)

The value of Neo-Hookean constant can be determined from the above equation. The values of Neo-Hookean constant should be determined for each case and average value must be taken as Neo-Hookean constant. The values of stress obtained using the Neo-Hookean model is thus determined.

### 3. Experimental Validation

Two sets of stress vs strain experimental data for materials “AN 70 O-ring at 165°C” and “GLS 70 at 175°C” were obtained under both compression and tension conditions. The specimen height was 50mm and cross-sectional area of 635mm<sup>2</sup>. The details of the experimental results and different models are discussed below. When the O-ring is placed inside the assembly, a part of the O-ring will undergo compression as a result of the applied load whereas the other part of the O-ring will suffer from tensile stress; therefore, both these modes have been considered in the analysis of the above proposed models.

Compression Mode: The values obtained for AN 70 O-ring are tabulated in Table 1. Deformation of specimen is from 2%-32% of its total length. To obtain elastic constant from Hooke's law, average value of force in each case was calculated.

The stretch ratio  $\lambda$  is a fundamental quantity to describe material deformation. It is defined as the current length (deformed length) divided by the original length (50mm). Stress values are calculated from the equation,

$$\text{Stress} = \frac{\text{average value of force}}{\text{initial cross sectional area}} \tag{35}$$

Strain values are calculated from the equation,

$$\text{Strain} = \frac{\text{final length} - \text{initial length}}{\text{initial length}} \tag{36}$$

From these stress-strain values elastic constants are determined from *Hooke's law*,

$$E = \frac{\text{stress}}{\text{strain}} \tag{37}$$

From the values of elastic constants, the specimen elastic constant is determined by taking the average value of elastic constants from each case. Value of elastic constant in this case is: 24.3031.

The constants for the Neo-Hookean and Mooney-Rivlin models were predicted using curve fit method using Eq. (21) and (22) respectively. The estimated value of constants and the stress values are shown in table 2.

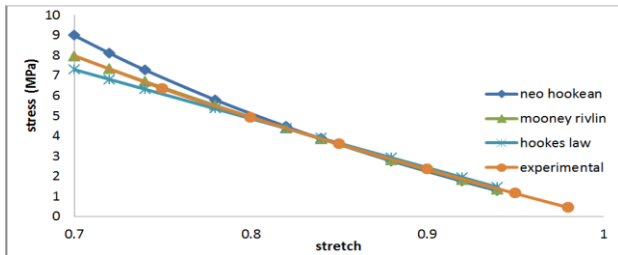
**Table 1:** Experimental Stress-strain values

Trial 1 (N)	Trial 2 (N)	Average force(N)	% of total height	Deformation(mm)	Deformed length	Stretch	Stress (MPa)	Strain	Elastic constant (MPa)
291.3	284.4	287.85	2%	1	49	0.98	0.453	0.02	22.6654
734.5	723.7	729.1	5%	2.5	47.5	0.95	1.148	0.05	22.6654
1499.4	1483.7	1491.55	10%	5	45	0.9	2.348	0.1	23.489
2294.8	2274.2	2284.5	15%	7.5	42.5	0.85	3.597	0.15	23.9843
3143.0	3108.7	3125.85	20%	10	40	0.8	4.922	0.2	24.613
4050.0	4012.9	4031.45	25%	12.5	37.5	0.75	6.348	0.25	25.395
5511.3	5466.2	5488.75	32%	16	34	0.68	8.643	0.32	27.0116

**Table 2:** Estimated value of constants and the stress values

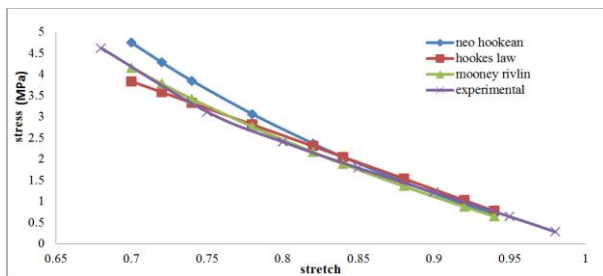
Neo-Hookean constant	Mooney-Rivlin constants	Intermediate values of deformation (mm)	Deformed length (mm)	Stretch	Strain	Neo-Hookean stress (MPa)	Mooney Rivlin stress (MPa)	Hooke's law (MPa)
-3.7015	C <sub>10</sub> =-5.12	3	47	0.94	0.06	1.2843	1.3501	1.46
-3.632	C <sub>01</sub> =1.509	4	46	0.92	0.08	1.7514	1.8229	1.94
-3.5103		6	44	0.88	0.12	2.7551	2.8062	2.91
-3.3681		8	42	0.84	0.16	3.8664	3.8439	3.89
-3.2279		9	41	0.82	0.18	4.469	4.3846	4.37
-3.0886		11	39	0.78	0.22	5.7849	5.5125	5.34
-2.915		13	37	0.74	0.26	7.2752	6.7055	6.31
		14	36	0.72	0.28	8.0981	7.327	6.80
		15	35	0.7	0.3	8.9809	7.9652	7.29

Comparison of stretch values for different values of stresses of experimental and intermediate values for all three models are plotted in figure 3. From this figure it can be observed that Mooney-Rivlin model estimates the value closest to the experimental value.



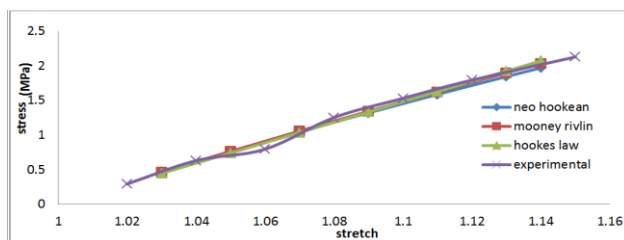
**Fig. 3** Comparison of stress vs stretch for AN 70 under compression

The test was repeated for GLS 70 O-Ring at 175°C in compression mode. The comparison of the results is shown in figure 4.

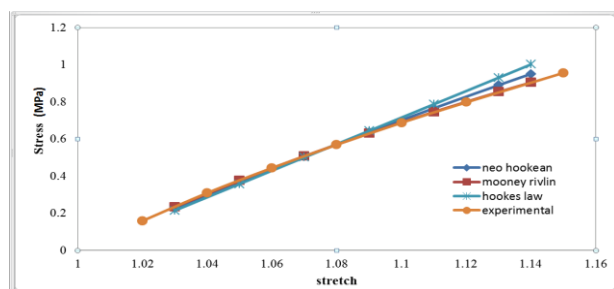


**Fig. 4** Comparison of stress vs stretch for GLS 70 under compression

Tension Mode: The similar test was repeated for samples in tension. The comparison of result is shown in figure 5(a) and (b) for AN 70 and GLS 70 respectively.



(a) AN 60



(b) GLS 70

**Fig. 5** Comparison of stress vs stretch for in-tension mode

It is inferred from the above plots that Mooney-Rivlin model is the best model which describes the behavior of materials in tension and compression compared to other theoretical models. Hence in the present work, Mooney-Rivlin model is used to estimate Young's Modulus.

Contact Width: Compression applied to the O-ring causes it to deform along the groove surface. The contact width thereafter generated has been described as a function of the squeeze imposed on the O-ring. The absence of the restraining effects of the lateral walls allows for the expansion of the O-ring along the radial direction.

$$Contact\ Width = 1.5 * \psi^{2/3} \tag{38}$$

Load per unit length: The elastic reaction of the O-ring under deformation, is the prime reason for the utilization of the O-ring for sealing purposes. With the increase in the compression within elastic limits, the load per unit length can be easily estimated as a function of the Young's Modulus cross-section diameter and the squeeze of the O-ring.

$$L = E * d * (1.25 * \psi^{1.5} + 50 * \psi^6) \tag{39}$$

After calculating the load per unit length, the total compressive force can be estimated by multiplying the load per unit length with the circumferential length ( $\pi * D$ ). This is represented in eq. (40).

$$Comp\_Force = \pi * L * D \tag{40}$$

Average stress over the O-ring: The primary sealing feature of an O-ring is the generation of contact stress upon deformation, which will be distributed over the contact width generated as a result of compression. The average stress can be evaluated using:

$$Stress = E * \sqrt{\frac{8}{3\pi} * [1.25 * \psi^{1.5} + 50 * \psi^6]} \tag{41}$$

Peak contact stress: The contact stress generated will be distributed in such a way that the maximum stress generated will be at the center of the contact width which will be evaluated using eq. (42).

$$MaxContStress = (E(2.62\psi - 8.85 \psi^2 + 12.83 \psi^3)) \tag{42}$$

The internal fluid sealed by the O-ring will exert pressure on the O-ring, thereby, deforming it further. This consequent deformation will result in increased contact pressure generation by the O-ring. This stress is known as hydro-stress and is expressed as the product of Poisson's ratio times the fluid pressure. This increase is calculated using eq. (43).

$$Hydrostress = v * P_1 \tag{43}$$

$$MaxContStressfluid = (E(2.62\psi - 8.85 \psi^2 + 12.83 \psi^3) + v * P_1) \tag{44}$$

### 4. Axially Loaded Lubricated Condition

Lubrication is provided to the O-ring in order to increase the life of the O-ring safeguarding the O-ring against wear and fatigue. When lubrication is provided to an O-ring, the fluid will tend to swell up the O-ring which will result in the increase in cross-section diameter of the O-ring. The increased diameter is then calculated taking into consideration the percentage of swell (sw) and thereafter using eq. (44).

$$d_1 = d\sqrt{1 + 0.01Sw} \tag{44}$$

Squeeze for lubricated O-ring after loading: With the change in diameter, the equivalent squeeze also changes and therefore, it is calculated using eq. (45).

$$squeeze = \psi * d_1 \tag{45}$$

Load per unit length for lubricated O-ring: The load changes with the change in the cross-sectional diameter and is given by the expression below:

$$L = E * d_1 * (1.25 * \psi^{1.5} + 50 * \psi^6) \tag{46}$$

After calculating the load per unit length, the total compressive force can be estimated by multiplying the load per unit length with the circumference ( $\pi * D$ ). This is represented in eq. (47).

$$Comp\_Force = \pi * L * D \tag{47}$$

The contact width and the contact stress generated for the O-ring have the same formula's which have been covered in Eq. (38), (41), (42), (43) and (44) respectively.

### 5. Radially Loaded O-Ring

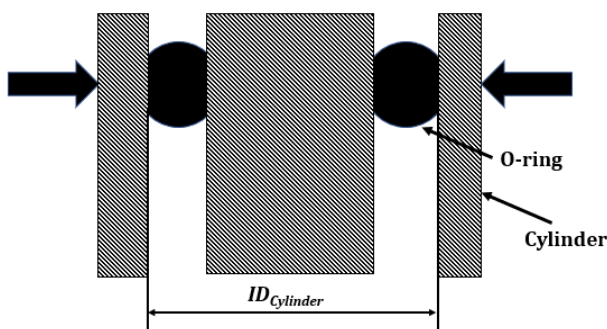


Fig. 6 Radial O-ring without Groove

The arrangement for the radial no groove arrangement is depicted in figure (6). The arrangement functions such that the O-ring is free to expand axially as a result of which the corresponding shape of the O-ring under load changes to the figure 7, given below:

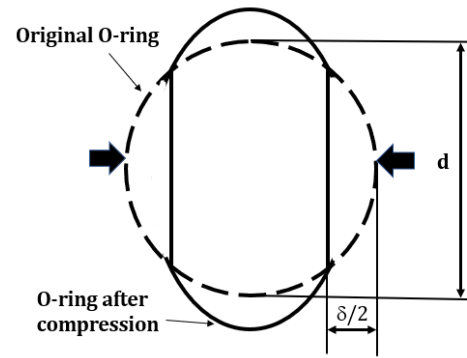


Fig. 7

Deformed shape of O-ring

The applied compression on the O-ring will result in the change in the cross-section of the O-ring as shown in figure (7). In order to define the change in the O-ring shape, a parameter called as Compression ratio ( $\psi$ ) is introduced which is defined as the change in the cross-sectional diameter divided by the original cross-sectional diameter.

$$\psi = \frac{Change\ in\ cross\text{-}sectional\ diameter}{Original\ diameter} \tag{48}$$

There are two possible installations of the O-ring into the assembly: (i) Unlubricated condition and (ii) Lubricated condition. Both of these conditions have been discussed separately.

### 6. Radially Loaded Unlubricated Condition

The unlubricated condition pertains to the installation of the O-ring inside the assembly without lubrication being provided to its surface. For static applications, where the movement between the sealing faces and the O-ring surface is negligible, unlubricated O-rings do not drastically affect the life of the O-ring.

Inner Diameter of the O-ring: The initial requirement are the inner diameter of the cylinder and the distance between the sealing faces for the calculation of the inner diameter of the O-ring.

$$ID_{O\text{-}ring} = ID_{Cylinder} - 2C \tag{49}$$

Squeeze: The O-ring under compression will undergo an effective squeeze which is calculated from the product of compression ratio ( $\psi$ ) and O-ring diameter ( $d$ ). The formulation is given in equation (50).

$$squeeze = \psi * d \tag{50}$$

Young's Modulus (E): The Young's Modulus for the O-ring can be calculated using two methods: (i) Using hardness and (ii) Using Stress-Strain values. Both of these methods have been discussed in detail earlier

Contact Width: The contact width is a function of the squeeze imposed on the O-ring. Contact width generated increases with the increase in the compression ratio and is given by eq. (51).

$$\text{Contact Width} = 1.5 * \psi^{2/3} \quad (51)$$

Load per unit length: With the increase in the compression within elastic limits, the load per unit length can be easily estimated as a function of the Young's Modulus cross-section diameter and the compression ration of the O-ring.

$$L = E * d * (1.25 * \psi^{1.5} + 50 * \psi^6) \quad (52)$$

After calculating the load per unit length, the total compressive force can be estimated by multiplying the load per unit length with the circumference ( $\pi * D$ ). This is represented in eq. (53).

$$\text{Comp\_Force} = \pi * L * D \quad (53)$$

Average stress over the O-ring: The contact stress generated will be distributed over the contact width. The average stress can be evaluated using:

$$\text{Stress} = E * \sqrt{\frac{8}{3\pi} * [1.25 * \psi^{1.5} + 50 * \psi^6]} \quad (54)$$

Peak contact stress: The contact stress generated will be distributed in such a way that the maximum stress generated will be at the center of the contact width which will be evaluated using eq. (55).

$$\text{MaxContStress} = (E(3.4\psi - 11.28\psi^2 + 21.75\psi^3)) \quad (55)$$

The sealed fluid pressure further deforms the O-ring and due to the elastic nature of the material, it results in an increase in the contact stress thereafter generated. This increase is calculated using eq. (56).

$$\text{Hydrostress} = v * P_1 \quad (56)$$

$$\text{MaxContStressfluid} = (E(3.4\psi - 11.28\psi^2 + 21.75\psi^3) + v * P_1) \quad (57)$$

## 7. Radially Loaded Lubricated Condition

When lubrication is provided to an O-ring, the fluid will tend to swell up the O-ring which will results in the increase in cross-section diameter of the O-ring. The increased diameter is then calculated taking into consideration the percentage of swell (sw) and thereafter using eq. (58).

$$d_1 = d\sqrt{1 + 0.015w} \quad (58)$$

Squeeze under lubricated conditions: With the change in diameter, the equivalent squeeze also changes and therefore, is calculated using eq. (59).

$$\text{squeeze} = \psi * d_1 \quad (59)$$

Load per unit length under lubrication: With the provision for the lubrication of the O-ring, the load per

unit length acting on the O-ring will vary as it is a function of the cross-section diameter of the O-ring. With the increase in the compression within elastic limits, the load per unit length can be easily estimated as a function of the Young's Modulus cross-section diameter and the squeeze of the O-ring.

$$L = E * d_1 * (1.25 * \psi^{1.5} + 50 * \psi^6) \quad (60)$$

After calculating the load per unit length, the total compressive force can be estimated by multiplying the load per unit length with the circumference ( $\pi * D$ ). This is represented in eq. (61).

$$\text{Comp\_Force} = \pi * L * D \quad (61)$$

The contact width and the contact stress generated for the O-ring have the same formula's which have been covered in Eq. (51), (54), (55), (56) and (57) respectively.

## Conclusion

In this paper, the design of the O-ring inside a no groove assembly has been considered. Both axial as well as radial loading of the O-ring has been taken into consideration with the case of a lubricated O-ring dealt with separately for each case. The design includes the calculation of the compression imposed upon the O-ring following which the values of the contact width, contact stress, and Young's Modulus were estimated. The effect of the sealed fluid pressure on the contact stress was also taken into consideration. Various tolerances involved during the design process were also incorporated.

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